

Name: Key

Date: _____

Transformations Review Sheet

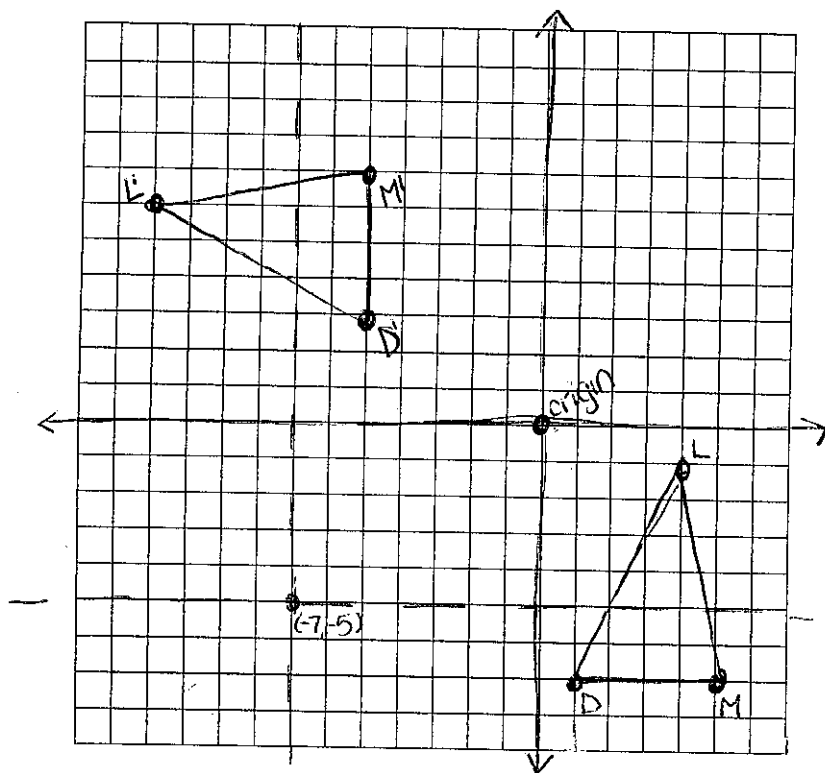
1. The point $(-2, 1)$ is rotated 180° about the origin in a clockwise direction. What are the coordinates of its image?

$(2, -1)$

2. Graph and state the coordinates of triangle $D'L'M'$ the image of triangle DLM after a rotation 90 degrees about point $R(-7, -5)$. Be sure to graph triangle DLM and show all the necessary steps to find the new coordinates.

$D(1, -7)$ $L(4, -1)$ $M(5, -7)$

$D'(-5, 3)$ $L'(-11, 6)$ $M'(-5, 7)$



WORK

$$(8, -2) \rightarrow (2, 8)$$

$$(12, -2) \rightarrow (2, 12)$$

$$(11, 4) \rightarrow (-4, 11)$$

(x, y) $(-y, -x)$

3. A transformation maps $(3, 5)$ onto $(-5, -3)$. This transformation is equivalent to a

(1) rotation of 90°

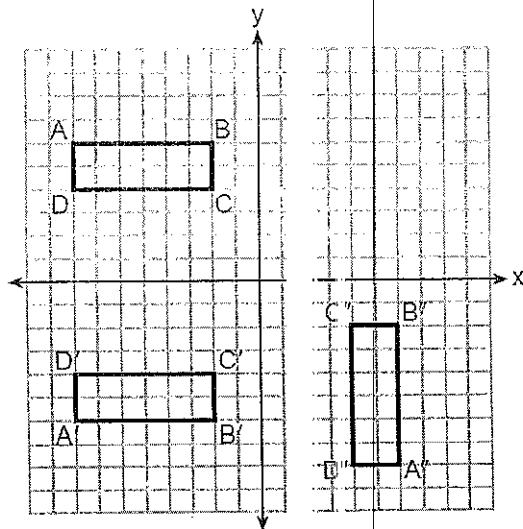
reflection in the line $y = -x$

(3) reflection in the line $y = x$

(4) translation of $-5, -3$

4.

A sequence of transformations maps rectangle $ABCD$ onto rectangle $A''B''C''D''$, as shown in the diagram below.



Which sequence of transformations maps $ABCD$ onto $A'B'C'D'$ and then maps $A'B'C'D'$ onto $A''B''C''D''$?

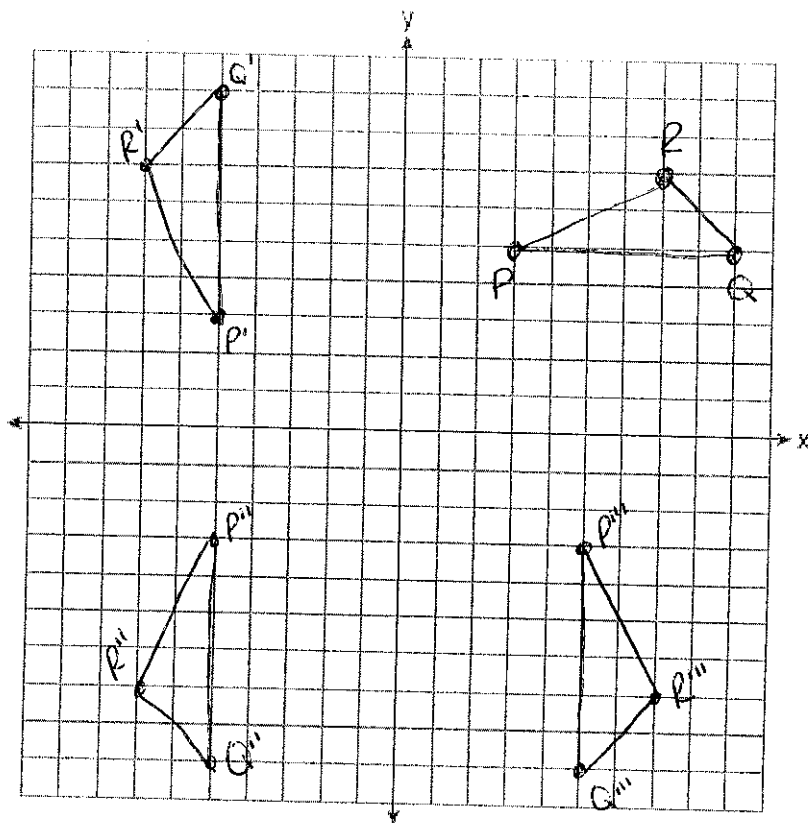
- (1) a reflection followed by a rotation
- (2) a reflection followed by a translation
- (3) a translation followed by a rotation
- (4) a translation followed by a reflection

5. A regular octagon is rotated clockwise around its center, the minimum number of degrees it must be rotated to carry the octagon onto itself is:

- (1) 45°
- (2) 72°
- (3) 108°
- (4) 360°

$360 \div 8 = 45$

11. On the graph below, draw and label $\triangle PQR$, whose vertices are $P(3, 5)$, $Q(9, 5)$, and $R(7, 7)$. On the same set of axes, graph and state the coordinates of
- $\triangle P'Q'R'$, the image of $\triangle PQR$ after R_{90° . $P'(-5, 3)$ $Q'(-5, 9)$ $R'(-7, 7)$
 - $\triangle P''Q''R''$, the image of $\triangle P'Q'R'$ after r_{x-axis} . $P''(-5, -3)$ $Q''(-5, -9)$ $R''(-7, -7)$
 - $\triangle P'''Q'''R'''$, the image of $\triangle P''Q''R''$ after r_{y-axis} . $P'''(5, -3)$ $Q'''(5, -9)$ $R'''(7, -7)$
- d) Based upon these graphs, write a single transformation that shows the composition $r_{y-axis} \circ r_{x-axis} \circ R_{90^\circ}$.

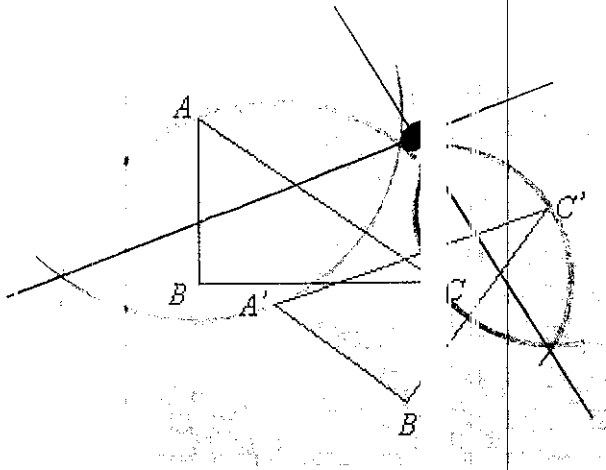


$$(3, 5) \rightarrow (5, -3)$$

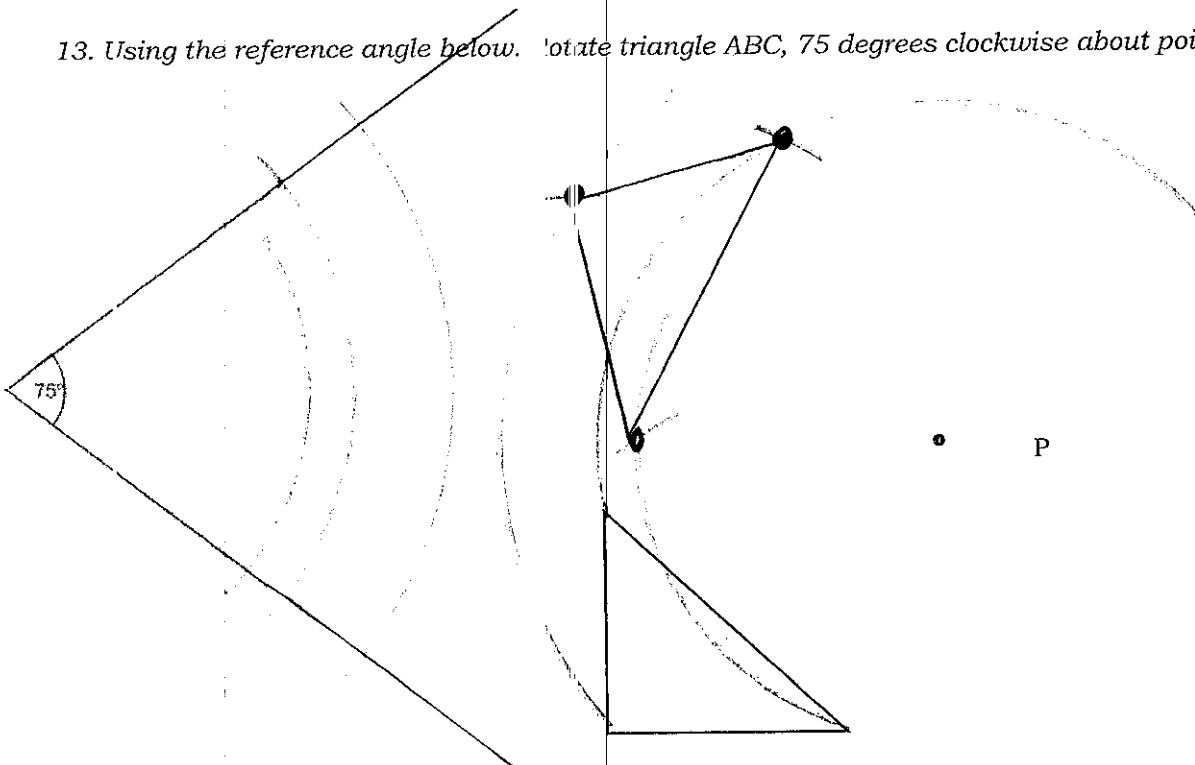
$$(x, y) \rightarrow (y, -x)$$

$$R_{270^\circ}$$

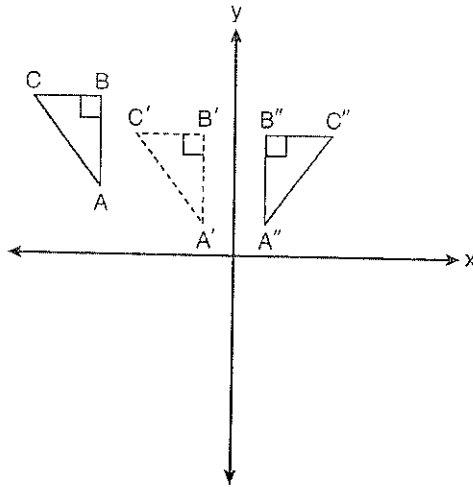
12. Using a compass and straightedge, find the center of rotation.



13. Using the reference angle below, rotate triangle ABC , 75 degrees clockwise about point P .

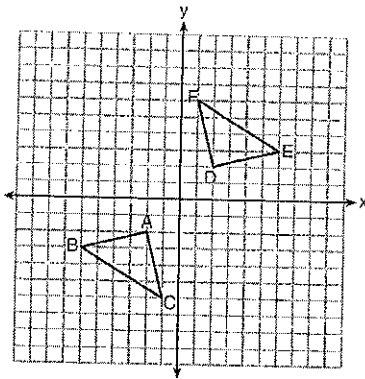


6. In the diagram below, $\triangle A'B'C'$ is a transformation of $\triangle ABC$, and $\triangle A''B''C''$ is a transformation of $\triangle A'B'C'$.



The composite transformation of $\triangle ABC$ to $\triangle A''B''C''$ is an example of a

- 1) reflection followed by a rotation
 - 2) reflection followed by a translation
 - 3) translation followed by a rotation
 - 4) translation followed by a reflection
7. Triangle ABC and triangle DEF are graphed on the set of axes below.



Which sequence of transformations maps triangle ABC onto triangle DEF ?

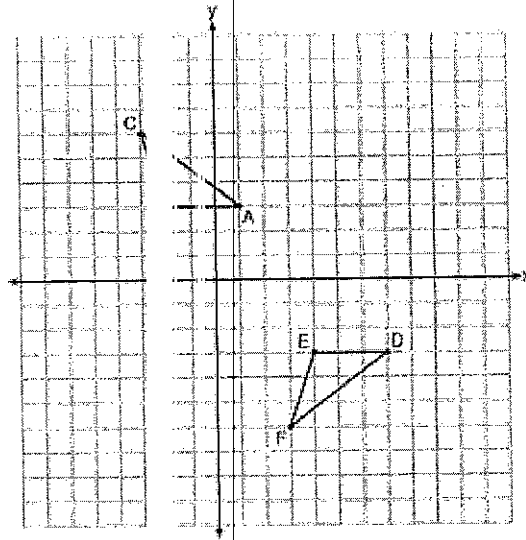
- 1) a reflection over the x -axis followed by a reflection over the y -axis
- 2) a 180° rotation about the origin followed by a reflection over the line $y = x$
- 3) a 90° clockwise rotation about the origin followed by a reflection over the y -axis
- 4) a translation 8 units to the right and 1 unit up followed by a 90° counterclockwise rotation about the origin

8. The image of $(4, 7)$ under a certain translation is the point $(2, -6)$. What is the image of point $(-3, -2)$ under the same translation?

$$(-3, -2) \rightarrow (-5, -15)$$

9.

Describe a sequence of transformations that will map $\triangle ABC$ onto $\triangle DEF$ as shown below.



a translation 6 units right followed by a reflection over the x-axis

10. Given: $\triangle MAD$ has coordinates $M(-3, 4)$, $A(2, 9)$, and $D(-1, -2)$.

a) State the coordinates of the vertices of $\triangle M'A'D'$, the image of $\triangle MAD$ under the composition

$R_{90^\circ} \circ r_{x\text{-axis}}$

$$M(-3, 4) \xrightarrow{r_{x\text{-axis}}} (-3, -4) \xrightarrow{R_{90^\circ}} M'(4, -3)$$

$$A(2, 9) \xrightarrow{r_{x\text{-axis}}} (2, -9) \xrightarrow{R_{90^\circ}} A'(9, 2)$$

$$D(-1, -2) \xrightarrow{r_{x\text{-axis}}} (-1, 2) \xrightarrow{R_{90^\circ}} D'(-2, -1)$$

$$(x, y) \rightarrow (y, x)$$

b) What single transformation is equivalent to $R_{90^\circ} \circ r_{x\text{-axis}}$?

$$r_{y=x}$$